

## EFFECT OF TEMPERATURE IN ANALYSIS OF CREEP IN AN ISOTROPIC UNIFORM COMPOSITE CYLINDER

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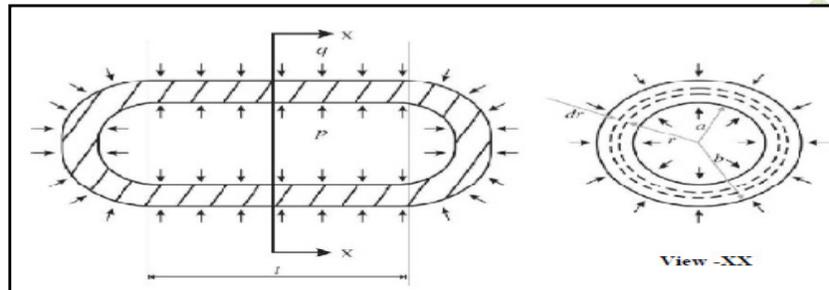
### ABSTRACT

The following paper discusses the effect of temperature in analysis of creep in an isotropic uniform composite cylinder. The paper is a part of the series of papers published under the analysis of creep in an isotropic uniform composite cylinder.

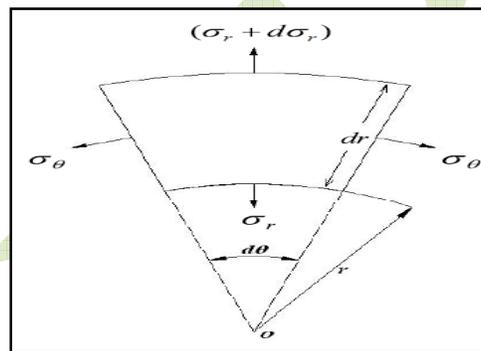
### INTRODUCTION

In applications such as pressure vessel for industrial gases or a media transportation of high-pressurized fluids and piping of nuclear reactors, the cylinder has to operate under severe mechanical and thermal loads, causing significant creep hence reduced service life (Gupta and Phatak, 2001; Tachibana and Iyoku, 2004; Hagihara and Miyazaki, 2008). As an example, in the high temperature engineering test reactor, the temperature reaches of the order of 900°C (Tachibana and Iyoku, 2004). The piping of reactor cooling system are subjected to high temperature and pressure and may be damaged due to high heat generated from the reactor core (Hagihara and Miyazaki, 2008). A number of studies pertaining to creep behaviour of the cylinder assume the cylinder to be made of monolithic material. However, under severe thermo mechanical loads cylinder made of monolithic materials may not perform well. The weight reduction achieved in engineering components, resulting from the use of aluminum/aluminum base alloys, is expected to save power and fuel due to a reduction in the payload of dynamic systems. However, the enhanced creep of aluminum and its alloys may be a big hindrance in such applications. Aluminum matrix composites offer a unique combination of properties, unlike many monolithic materials like metals and alloys, which can be tailored by modifying the content of reinforcement. Experimental studies on creep under uniaxial loading have demonstrated that steady state creep rate is reduced by several orders of magnitude in aluminum or its alloys reinforced with ceramic particles/whiskers like silicon carbide as compared to pure aluminum or its alloys (Nieh, 1984; Nieh *et al*, 1988). A significant improvement in specific strength and stiffness may also be attained in composites based on aluminum and aluminum alloys containing silicon carbide particles or whiskers. In addition, a suitable choice of variables such as reinforcement geometry, size and content of reinforcement in these composites can be used to make the cost-effective components with improved performance. With these forethoughts, it is decided to investigate the steady state creep in a cylinder made of Al-SiCp composite and subjected to high pressure and high temperature. A mathematical model has been

developed to describe the steady state creep behavior of the composite cylinder. The developed model is used to investigate the effect of material parameters viz particle size and particle content, and operating temperature on the steady state creep response of the composite cylinder.



**Fig. Schematic of closed end, thick-walled composite cylinder subjected to internal and external pressures.**

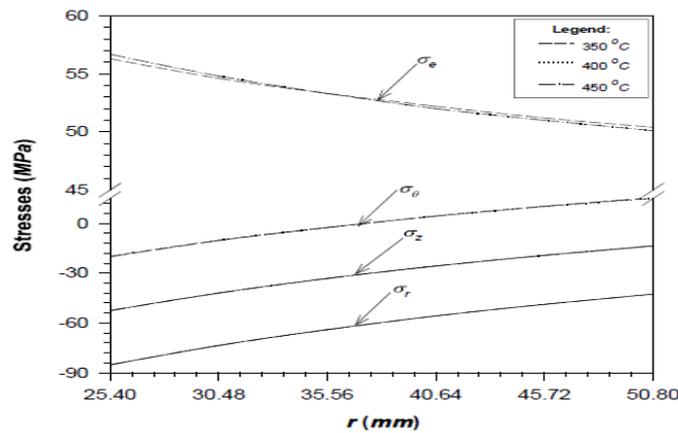


**Fig. Free body diagram of an element of the composite cylinder**

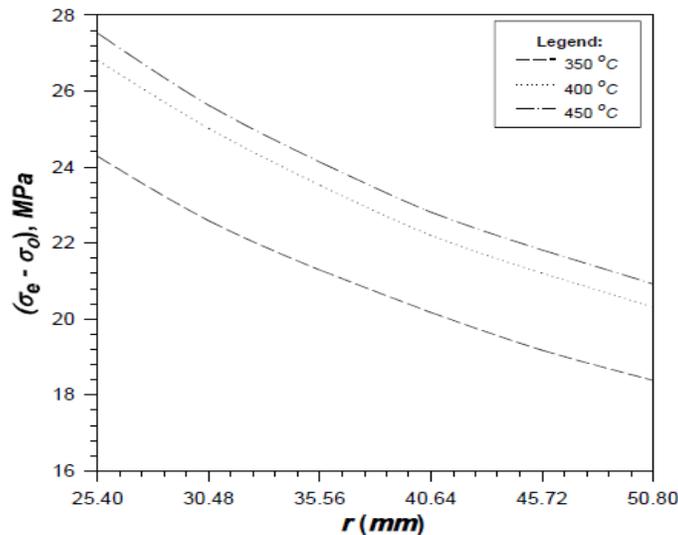
## EFFECT OF TEMPERATURE

The creep in a material is significantly influenced by the operating temperature. Therefore, this section brings out the effect of varying operating temperature on the stresses and strain rates in a thick cylinder made of aluminum matrix composite reinforced with 20 vol% of SiCp. Figure 1 shows the variation of radial, tangential, axial and effective stresses in a composite cylinder operating at three different temperatures *i.e.* 350 oC, 400 oC and 450 oC. Similar to the effect observed for particle size (Fig. 2), the radial, tangential and axial stresses do not exhibit sizable variation with the increase in operating temperature from 350 oC to 450 oC. The effect of temperature on the stresses is not significant, except for a slight variation noticed for effective stress. With the decrease in operating temperature from 450 oC to 350 oC, the compressive value of tangential stress increases a little (around 2.5%) near the inner radius. It is interesting to observe that in the middle of cylinder, the nature of tangential stress changes from compressive to tensile. Further, this tensile value of tangential stress increases on moving towards the outer radius of cylinder with the decrease in operating temperature from 450 oC to 350 oC. The maximum increase observed is around 3%. The variation of axial stress is similar to that observed for radial stress. It remains compressive throughout the cylinder, with maximum value

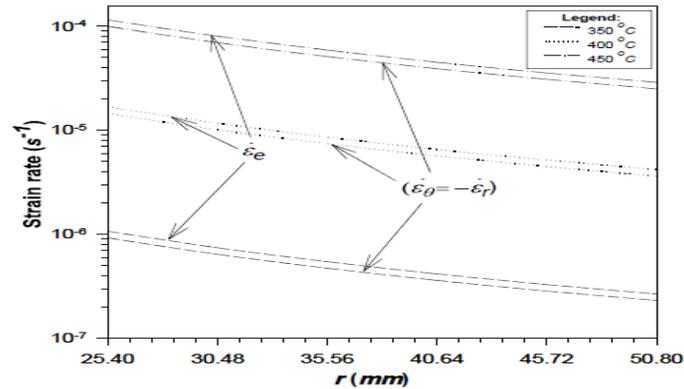
at the inner radius and minimum value at the outer radius. On the other hand, the effective stress, near the inner radius, decreases marginally with the decrease in temperature from 450 oC to 350 oC; but it exhibits a marginal increase towards the outer radius with the decrease in temperature. The stress difference ( $\sigma_e - \sigma_0$ ) shown in Fig. 3.13, decreases throughout the cylinder with decreasing temperature. The maximum decrease observed in stress difference is around 12% over the entire radius when the operating temperature decreases from 450 oC to 350 oC. The effective, radial and tangential strain rates in the cylinder decreases by about two orders of magnitude with the decrease in operating temperature from 450 oC to 350 oC. With decrease in operating temperature, the threshold stress  $\sigma_0$  increases and the creep parameter  $M$  decreases (Table 1), as a result of which the strain rates in the composite cylinder decrease to a significant extent. The effect of temperature on the creep rate observed in this study are similar to those reported by Pandey *et al* (1992) for Al- SiCp composites under uniaxial creep



**Fig no 1 Variation of creep stresses in composite cylinder for varying temperature ( $V = 20$  vol%,  $P = 1.7 \mu\text{m}$ ).**



**Fig No. 2 Variation of stress difference in composite cylinder for varying operating temperature ( $V = 20$  vol%,  $P = 1.7 \mu\text{m}$ ).**



**Fig no 3 Variation of strain rates in composite cylinder for varying operating temperature ( $V = 20 \text{ vol}\%$ ,  $P = 1.7\mu\text{m}$ ).**

## SELECTION OF MATERIAL PARAMETERS

It is evident from the above discussion that the creep stresses in a thick composite cylinder do not vary significantly by varying size and content of reinforcement (SiCp) as compared to the variation observed in strain rates. From The point of view of designing composite pressure vessel, operating under elevated temperature, the strain rates are considered to be primary design parameters. In order to reduce the steady state creep rates in the composite Cylinder, working under a given set of operating conditions (*i.e.* operating pressure and temperature) any of the following three options could be employed: (i) using finer size of reinforcement (SiCp) without varying its content, (ii) incorporating higher amount of dispersoids (SiCp) without altering its size, and (iii) simultaneously decreasing the size and increasing the amount of SiCp reinforcement. The selection of optimum size and content of the reinforcement in a composite pressure vessel, working under a given set of operating conditions, can be decided by simultaneously optimizing the cost of composite and the value of maximum strain rate in the composite cylinder for different combinations of particle size and particle content within the specified range.

## RESULTS AND DISCUSSION

Numerical calculations have been carried out to obtain the steady state creep response of the composite cylinder for different particle size, particle content and operating temperature.

## VALIDATION

Before discussing the results obtained, it is necessary to check the accuracy of analysis carried out and the computer program developed. To accomplish this task, the tangential, radial and axial stresses have been computed from the current analysis for a copper cylinder, the results for which are available in literature (Johnson *et al*, 1961). The dimensions of the cylinder, operating

pressure and temperature, and the values of creep parameters used for the purpose of validation are summarized in Table 2.

**Table no.2 Summary of data used for validation (Johnson et al)**

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Cylinder Material : Copper

Cylinder dimensions:  $a = 25.4 \text{ mm}$ ,  $b = 50.8 \text{ mm}$ .

Internal Pressure = 23.25 MPa, External Pressure = 0

Operating Temperature = 250 °C

Creep parameters estimated:  $M = 3.271 \times 10^{-4} \text{ s}^{-1/5} / \text{MPa}$ ,  $\sigma_0 = 11.32 \text{ MPa}$

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To estimate the values of parameters  $M$  and  $\sigma_0$  for copper cylinder, firstly  $\sigma_e$  have been calculated at the inner and outer radii of the cylinder by substituting the values of  $\sigma_e$ ,  $\sigma_r$ ,  $\sigma_\theta$ ,  $\sigma_z$  in Eqn. we obtained at these locations, as reported in The study of Johnson *et al* (1961). The values of stresses  $\sigma_r$ ,  $\sigma_\theta$  and  $\sigma_z$  and the tangential strain rate  $\dot{\epsilon}_\theta$  reported by Johnson *et al* (1961) at the inner and outer radii are substituted in Eqn. we know to estimate the effective strain rates at the corresponding radial locations. The effective stresses and effective strain rates thus estimated at the inner radius  $\sigma_e = 189.83 \text{ MPa}$  and  $\dot{\epsilon}_e = 2.168 \times 10^{-8} \text{ s}^{-1}$  and at the outer radius  $\sigma_e = 116 \text{ MPa}$   $\dot{\epsilon}_e = 1.128 \times 10^{-9} \text{ s}^{-1}$  of the copper cylinder are substituted in creep law, Eqn. we obtained, to obtain the creep parameters  $M$  and  $\sigma_0$  for copper cylinder as given in Table 3.2. These creep parameters have been used in the developed software to compute the distribution of tangential strain rate in the copper cylinder. The tangential strain rates, thus obtained, have been compared with those reported by Johnson *et al* (1961). A nice agreement is observed in Fig. 3 verifies the accuracy of analysis presented and software developed in the current study.

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